

## Abulwafa, EM DEC 2012

### Time-fractional study of electron acoustic solitary waves in plasma of cold electron and two isothermal ions

Author(s): [El-Wakil, SA](#) (El-Wakil, S. A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [El-Shewy, EK](#) (El-Shewy, Emad K.)<sup>[1,2]</sup>; [Mahmoud, AA](#) (Mahmoud, Abeer A.)<sup>[1]</sup>

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#### Abstract:

In this paper, a homogeneous system of unmagnetized collisionless plasma consisting of a cold electron fluid, low-temperature ion obeying Boltzmann-type distribution and high-temperature ion obeying non-thermal distribution is considered. The perturbation method with two different forms of stretching will be considered to drive the KdV and modified KdV (mKdV) equations. The Agrawal's method is applied to formulate the time-fractional KdV and mKdV equations. A variational iteration method is used to solve these equations. The results show that the fractional order of the differential equations can be used to modify the shape of the solitary pulse instead of adding higher order dissipation terms to the equations. This study may be useful to construct the compressive and rarefactive electrostatic potential pulses associated with the broadband electrostatic noise type emissions.

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Reprint Address: El-Wakil, SA (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Grp, Mansoura, Egypt.

#### Addresses:

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Grp, Mansoura, Egypt

[ 2 ] Qassim Univ, Sci & Arts Coll Al Rass, Dept Phys, Buraydah, Al Rass Provinc, Saudi Arabia

E-mail Address: [abulwafa@mans.edu.eg](mailto:abulwafa@mans.edu.eg)

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Ion-acoustic waves in unmagnetized collisionless weakly relativistic plasma of warm-ion and isothermal-electron using time-fractional KdV equation

Author(s): [El-Wakil, SA](#) (El-Wakil, Sayed A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [El-Shewy, EK](#) (El-Shewy, Emad K.)<sup>[1]</sup>; [Mahmoud, AA](#) (Mahmoud, Aber A.)<sup>[1]</sup>

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**Abstract:**

Collisionless unmagnetized plasma consisting of a mixture of warm ion-fluid and isothermal-electron is considered, assuming that the ion flow velocity has a weak relativistic effect. The reductive perturbation method has been employed to derive the Korteweg-de Vries (KdV) equation for small - but finite-amplitude electrostatic ion-acoustic waves in this plasma. The semi-inverse method and Agrawal's method lead to the Euler-Lagrange equation that leads to the time fractional KdV equation. The variational-iteration method given by He is used to solve the derived time fractional KdV equation. The calculations show that the fractional order may play the same rule of higher order dissipation in KdV equation to modulate the soliton wave amplitude in the plasma system. The results of the present investigation may be applicable to some plasma environments, such as space-plasmas, laser-plasma interaction, plasma sheet boundary layer of the earth's magnetosphere, solar atmosphere and interplanetary space. (C) 2012 COSPA R. Published by Elsevier Ltd. All rights reserved.

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Reprint Address: Abulwafa, EM (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt

E-mail Address: [abulwafa@mans.edu.eg](mailto:abulwafa@mans.edu.eg)

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 Author(s): NEJOH, Y  
 Source: JOURNAL OF PLASMA PHYSICS Volume: 37 Pages: 487-495 Part: Part 3 Abstract Number: A1987-123973 Published: JUN 1987
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 Author(s): PAKIRA, GP; CHOWDHURY, AR; PAUL, SN  
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 Author(s): Podlubny, I.  
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 Author(s): Sabatier, J.; Agrawal, O. P.; Tenreiro Machado, J. A.  
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 Author(s): Sanchez, R.; Carreras, B. A.; Newman, D. E.; et al.  
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 Author(s): Vette, J.I.  
 Book Editor(s): McCormac, B.M.  
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 Published: 1970
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 Author(s): WASHIMI, H; TANIUTI, T  
 Source: PHYSICAL REVIEW LETTERS Volume: 17 Issue: 19 Pages: 996-& DOI: 10.1103/PhysRevLett.17.996 Abstract Number: A1967-04244 Published: 1966

## El-Wakil, SA SEP 2011

### Time-fractional KdV equation for plasma of two different temperature electrons and stationary ion

Author(s): [El-Wakil, SA](#) (El-Wakil, S. A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [El-Shewy, EK](#) (El-Shewy, E. K.)<sup>[1]</sup>; [Mahmoud, AA](#) (Mahmoud, Abeer A.)<sup>[1]</sup>

Source: PHYSICS OF PLASMAS Volume: 18 Issue: 9 Article Number: 092116 DOI: 10.1063/1.3640533 Published: SEP 2011

#### Abstract:

Using the time-fractional KdV equation, the nonlinear properties of small but finite amplitude electron-acoustic solitary waves are studied in a homogeneous system of unmagnetized collisionless plasma. This plasma consists of cold electrons fluid, non-thermal hot electrons, and stationary ions. Employing the reductive perturbation technique and the Euler-Lagrange equation, the time-fractional KdV equation is derived and it is solved using variational method. It is found that the time-fractional parameter significantly changes the soliton amplitude of the electron-acoustic solitary waves. The results are compared with the structures of the broadband electrostatic noise observed in the dayside auroral zone. (C) 2011 American Institute of Physics.

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**KeyWords** Plus: ACOUSTIC SOLITARY WAVES; BAND ELECTROSTATIC NOISE; DOUBLE-LAYERS; VARIATIONAL-PRINCIPLES; PROPAGATION; GENERATION; AMPLITUDE; SOLITONS

Reprint Address: El-Wakil, SA (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt.

#### Addresses:

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt

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Author(s): Agrawal, OP

Source: JOURNAL OF MATHEMATICAL ANALYSIS AND APPLICATIONS Volume: 272 Issue: 1 Pages: 368-379 Article Number: PII S0022-247X(02)00180-4 DOI: 10.1016/S0022-247X(02)00180-4 Abstract Number: A2003-01-0230-015 Published: AUG 1 2002

2. Title: Fractional variational calculus in terms of Riesz fractional derivatives Author(s): Agrawal, O. P.

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Editor(s): Baleanu, D.; Guvenc, Z. B.; Tenreiro Machado, J. A.

Source: New Trends in Nanotechnology and Fractional Calculus Applications Published: 2010  
Publisher: Springer

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Author(s): Baleanu, Dumitru; Machado, J. A. Tenreiro

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Author(s): BOSTROM, R; GUSTAFSSON, G; HOLBACK, B; et al.

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Author(s): Bounds, SR; Pfaff, RF; Knowlton, SF; et al.

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Author(s): del-Castillo-Negrete, D; Carreras, BA; Lynch, VE

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Author(s): DUBOULOZ, N; POTTELETTE, R; MALINGRE, M; et al.

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Author(s): DUBOULOZ, N; TREUMANN, RA; POTTELETTE, R; et al.

Source: JOURNAL OF GEOPHYSICAL RESEARCH-SPACE PHYSICS Volume: 98 Issue: A10 Pages: 17415-17422 DOI: 10.1029/93JA01611 Abstract Number: A1994-01-9420-023 Published: OCT 1 1993

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Author(s): DUBOULOZ, N; POTTELETTE, R; MALINGRE, M; et al.

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Author(s): El-Shewy, E. K.

Conference: Conference on elnaschie Nonlinear Dynamics Location: Shanghai, PEOPLES R CHINA Date: 2005

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Source: CHAOS SOLITONS & FRACTALS Volume: 26 Issue: 4 Pages: 1073-1079 DOI: 10.1016/j.chaos.2005.01.060 Published: NOV 2005

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Author(s): El-Wakil, S. A.; Abulwafa, E. M.; Zahran, M. A.; et al.

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Author(s): Ergun, RE; Carlson, CW; McFadden, JP; et al.

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Author(s): Gustafson, K.; del-Castillo-Negrete, D.; Dorland, W.

Source: PHYSICS OF PLASMAS Volume: 15 Issue: 10 Article Number: 102309 DOI: 10.1063/1.3003072 Published: OCT 2008

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Author(s): He, JH

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Author(s): He, J.H.

Source: Commun. Nonlinear Sci. Numer. Simulat. Volume: 2 Issue: 4 Pages: 230-235 DOI: 10.1016/S1007-5704(97)90007-1 Published: 1997

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Author(s): HENRY, D; TREGUIER, JP

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Author(s): Mamun, AA; Shukla, PK

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Author(s): Mozer, FS; Ergun, R; Temerin, M; et al.

Source: PHYSICAL REVIEW LETTERS Volume: 79 Issue: 7 Pages: 1281-1284 DOI: 10.1103/PhysRevLett.79.1281 Abstract Number: A1997-20-9430-005 Published: AUG 18 1997

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Author(s): Pottellette, R; Ergun, RE; Treumann, RA; et al.

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Author(s): Sahu, Biswajit  
Source: PHYSICS OF PLASMAS Volume: 17 Issue: 12 Article Number: 122305 DOI: 10.1063/1.3527988 Published: DEC 2010

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Author(s): Sahu, B; Roychoudhury, R  
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Abstract Number: A2004-12-5235-035 Published: MAY 2004

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Author(s): SAMKO SG  
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Author(s): Sanchez, R.; Carreras, B. A.; Newman, D. E.; et al.  
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Author(s): Singh, SV; Reddy, RV; Lakhina, GS  
Book Editor(s): Malingre, M  
Conference: D3 2 Symposium of COSPAR Scientific Commission D held at the 33rd COSPAR Scientific Assembly Location: WARSAW, POLAND Date: JUL, 2000  
Sponsor(s): Amer Geophys Union; Ctr Natl Etud Spatiales; Int Union Radio Sci; Int Union Geodesy & Geophys; Int Assoc Geomagnet Aeronom; Comm Space Res  
Source: ADVANCES IN AURORAL PHYSICS Book Series: ADVANCES IN SPACE RESEARCH Volume: 28 Issue: 11 Pages: 1643-1648 DOI: 10.1016/S0273-1177(01)00479-3 Published: 2001

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Author(s): Singh, SV; Lakhina, GS  
Conference: 5th International Workshops on Nonlinear Waves and Chaos in Space Plasmas Location: Mumbai, INDIA Date: MAR 02-07, 2003  
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Author(s): Singh, SV; Lakhina, GS  
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Author(s): TEMERIN, M; CERNY, K; LOTKO, W; et al.  
Source: PHYSICAL REVIEW LETTERS Volume: 48 Issue: 17 Pages: 1175-1179 DOI: 10.1103/PhysRevLett.48.1175 Abstract Number: A1982-071191 Published: 1982

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Author(s): Tribeche, Mouloud; Djebarni, Lyes  
Source: PHYSICS OF PLASMAS Volume: 17 Issue: 12 Article Number: 124502 DOI: 10.1063/1.3522777 Published: DEC 2010

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Author(s): WASHIMI, H; TANIUTI, T  
Source: PHYSICAL REVIEW LETTERS Volume: 17 Issue: 19 Pages: 996-& DOI: 10.1103/PhysRevLett.17.996 Abstract Number: A1967-04244 Published: 1966

**EI-Wakil, SA JUL 2011**

**Time-fractional KdV equation: formulation and solution using variational methods**

Author(s): [EI-Wakil, SA](#) (EI-Wakil, S. A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, E. M.)<sup>[1]</sup>; [Zahran, MA](#) (Zahran, M. A.)<sup>[1]</sup>; [Mahmoud, AA](#) (Mahmoud, A. A.)<sup>[1]</sup>

Source: NONLINEAR DYNAMICS Volume: 65 Issue: 1-2 Pages: 55-63 DOI: 10.1007/s11071-010-9873-5  
Published: JUL 2011

**Abstract:**

In this work, the semi-inverse method has been used to derive the Lagrangian of the Korteweg-de Vries (KdV) equation. Then the time operator of the Lagrangian of the KdV equation has been transformed into fractional domain in terms of the left-Riemann-Liouville fractional differential operator. The variational of the functional of this Lagrangian leads neatly to Euler-Lagrange equation. Via Agrawal's method, one can easily derive the time-fractional KdV equation from this Euler-Lagrange equation. Remarkably, the time-fractional term in the resulting KdV equation is obtained in Riesz fractional derivative in a direct manner. As a second step, the derived time-fractional KdV equation is solved using He's variational-iteration method. The calculations are carried out using initial condition depends on the nonlinear and dispersion coefficients of the KdV equation. We remark that more pronounced effects and deeper insight into the formation and properties of the resulting solitary wave by additionally considering the fractional order derivative beside the nonlinearity and dispersion terms.

Accession Number: WOS:000291923500004

Document Type: Article

Language: English

Author Keywords: Riemann-Liouville fractional differential operator; Euler-Lagrange equation; Riesz fractional derivative; Fractional KdV equation; He's variational-iteration method; Solitary wave

**KeyWords** Plus: DIFFERENTIAL-EQUATIONS; CLASSICAL FIELDS; DERIVATIVES; CALCULUS; PRINCIPLES; MECHANICS; EXISTENCE; MEDIA; ORDER

Reprint Address: Abulwafa, EM (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt

E-mail Address: [emabulwafa@gmail.com](mailto:emabulwafa@gmail.com)

Publisher: SPRINGER, VAN GODEWIJCKSTRAAT 30, 3311 GZ DORDRECHT, NETHERLANDS

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Research Areas: Engineering; Mechanics

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 Author(s): Agrawal, OP  
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 Author(s): Agrawal, O. P.  
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 Author(s): AGRAWAL OP  
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5. Title: A general formulation and solution scheme for fractional optimal control problems  
 Author(s): Agrawal, OP  
 Source: NONLINEAR DYNAMICS Volume: 38 Issue: 1-4 Pages: 323-337 DOI: 10.1007/s11071-004-3764-6 Abstract Number: A2005-14-0230-031; C2005-07-1330-062 Published: DEC 2004
  
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 Author(s): Attari, Mina; Haeri, Mohammad; Tavazoei, Mohammad Saleh  
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 Author(s): Baleanu, Dumitru; Trujillo, Juan I.  
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 Author(s): Baleanu, D; Avkar, T  
 Source: NUOVO CIMENTO DELLA SOCIETA ITALIANA DI FISICA B-GENERAL PHYSICS RELATIVITY ASTRONOMY AND MATHEMATICAL PHYSICS AND METHODS Volume: 119 Issue: 1 Pages: 73-79 DOI: 10.1393/ncb/i2003-10062-y Abstract Number: A2005-06-0230-018 Published: JAN 2004



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 Author(s): Baleanu, D; Muslih, SI  
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 Author(s): Baleanu, Dumitru  
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 Author(s): Bateman, H  
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 Author(s): DELBOSCO D  
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 Author(s): Frederico, Gastao S. F.; Torres, Delfim F. M.  
 Conference: 2nd Workshop on Fractional Differentiation and Its Applications (FDA '06) Location: Oporto, PORTUGAL Date: JUL 19-21, 2006  
 Sponsor(s): IFAC  
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 Author(s): Fung, MK  
 Conference: Meeting in Honour of Dr Ta-You Wus Birthday Location: TAIPEI, TAIWAN Date: AUG 11-15, 1997  
 Sponsor(s): Academia Sin, Inst Phys; Natl Sci Council R O C, Nat Sci Div, Phys Res Promot Ctr; Phys Soc Republic China  
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 Author(s): He, JH  
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Author(s): He, JH

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Author(s): He, JH

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Source: INTERNATIONAL JOURNAL OF TURBO & JET-ENGINES Volume: 14 Issue: 1 Pages: 23-28  
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Author(s): Herzallah, Mohamed A. E.; Baleanu, Dumitru

Source: NONLINEAR DYNAMICS Volume: 58 Issue: 1-2 Pages: 385-391 DOI: 10.1007/s11071-009-9486-z  
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Author(s): Heymans, N

Source: NONLINEAR DYNAMICS Volume: 38 Issue: 1-4 Pages: 221-231 DOI: 10.1007/s11071-004-3757-5  
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Author(s): Inokuti, M.; Sekine, H.; Mura, T.

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Author(s): Korteweg, DJ; de Vries, G.

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Author(s): LUCHKO, YF; SRIVASTAVA, HM

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 Author(s): Tenreiro Machado, J. A.  
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 Author(s): Vilela Mendes, R.  
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32. Title: Hamiltonian formulation of classical fields within Riemann-Liouville fractional derivatives  
 Author(s): Muslih, SI; Baleanu, D; Rabei, E  
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 Author(s): Rabei, Eqab M.; Altarazi, Ibrahim M. A.; Muslih, Sami I.; et al.  
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 Author(s): Sabatier, J.; Agrawal, O. P.; Tenreiro Machado, J. A.

Source: ADV FRACTIONAL CALCULUS Published: 2007  
Publisher: Springer, New York, NY, USA

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Author(s): SAMKO SG

Source: FRACTIONAL INTEGRALS Published: 1998

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Author(s): Tarasov, Vasily E.; Zaslavsky, George M.

Source: JOURNAL OF PHYSICS A-MATHEMATICAL AND GENERAL Volume: 39 Issue: 31 Pages: 9797-9815 DOI: 10.1088/0305-4470/39/31/010 Published: AUG 4 2006

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Author(s): Tarasov, VE; Zaslavsky, GM

Source: PHYSICA A-STATISTICAL MECHANICS AND ITS APPLICATIONS Volume: 354 Pages: 249-261  
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Author(s): Tavazoei, Mohammad Saleh; Haeri, Mohammad

Source: NONLINEAR DYNAMICS Volume: 57 Issue: 3 Pages: 363-373 DOI: 10.1007/s11071-008-9447-y Published: AUG 2009

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Author(s): Zhang, SQ

Source: JOURNAL OF MATHEMATICAL ANALYSIS AND APPLICATIONS Volume: 278 Issue: 1 Pages: 136-148 DOI: 10.1016/S0022-247X(02)00583-8 Published: FEB 1 2003

**Abulwafa, EM MAY 2011**

**Time-fractional KdV equation for electron-acoustic waves in plasma of cold electron and two different temperature isothermal ions**

Author(s): [El-Wakil, SA](#) (El-Wakil, Sayed A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [El-shewy, EK](#) (El-shewy, Emad K.)<sup>[1]</sup>; [Mahmoud, AA](#) (Mahmoud, Abeer A.)<sup>[1]</sup>

Source: ASTROPHYSICS AND SPACE SCIENCE Volume: 333 Issue: 1 Pages: 269-276 DOI: 10.1007/s10509-011-0629-6 Published: MAY 2011

**Abstract:**

The time fractional KdV equation is derived for small but finite amplitude electron-acoustic solitary waves in plasma of cold electron fluid with two different temperature isothermal ions. The effects of the time fractional parameter on the electrostatic solitary structures are presented. It is shown that the effect of time fractional parameter can be used to modify the amplitude of the electrostatic waves (viz. the amplitude, width and electric field) of the electron-acoustic solitary waves. The model may provide a possible explanation for the low-frequency component of the broadband electrostatic noise in the plasma sheet boundary layer of the Earth's magnetotail where the electron beams are not present.

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Language: English

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**KeyWords Plus:** SOLITARY WAVES; NONTHERMAL ELECTRONS; EARTHS MAGNETOTAIL; DERIVATIVES; MECHANICS; AMPLITUDE; SOLITONS

Reprint Address: Abulwafa, EM (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt

E-mail Address: [abulwafa@mans.edu.eg](mailto:abulwafa@mans.edu.eg)

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**Abulwafa, EM APR 2011**

**Ion-acoustic waves in plasma of warm ions and isothermal electrons using time-fractional KdV equation**

Author(s): [El-Wakil, SA](#) (El-Wakil, Sayed A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [El-Shewy, EK](#) (El-Shewy, Emad K.)<sup>[1]</sup>; [Mahmoud, AA](#) (Mahmoud, Abeer A.)<sup>[1]</sup>

Source: CHINESE PHYSICS B Volume: 20 Issue: 4 Article Number: 040508 DOI: 10.1088/1674-1056/20/4/040508 Published: APR 2011

**Abstract:** The ion-acoustic solitary wave in collisionless unmagnetized plasma consisting of warm ions-fluid and isothermal electrons is studied using the time fractional KdV equation. The reductive perturbation method has been employed to derive the Korteweg-de Vries equation for small but finite amplitude ion-acoustic wave in warm plasma. The Lagrangian of the time fractional KdV equation is used in a similar form to the Lagrangian of the regular KdV equation with fractional derivative for the time differentiation. The variation of the functional of this Lagrangian leads to the Euler-Lagrange equation that gives the time fractional KdV equation. The variational-iteration method is used to solve the derived time fractional KdV equation. The calculations of the solution are carried out for different values of the time fractional order. These calculations show that the time fractional can be used to modulate the electrostatic potential wave instead of adding a higher order dissipation term to the KdV equation. The results of the present investigation may be applicable to some plasma environments, such as the ionosphere plasma.

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Language: English

Author Keywords: ion-acoustic waves; Euler-Lagrange equation; Riemann-Liouville fractional derivative; fractional KdV equation; variational-iteration method

**KeyWords Plus:** VARIATIONAL-ITERATION METHOD; DIFFERENTIAL-EQUATIONS; CLASSICAL FIELDS; SOLITARY WAVES; DERIVATIVES; FORMULATION; MECHANICS; PROPAGATION; PRINCIPLES; MEDIA

Reprint Address: El-Wakil, SA (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Phys Res Grp, Mansoura 35516, Egypt

E-mail Address: [elwakil@mans.edu.cn](mailto:elwakil@mans.edu.cn)

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Research Areas: Physics

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Author(s): Wu, Guo-cheng; Lee, E. W. M.  
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10.1016/j.physleta.2010.04.034 Published: MAY 31 2010

**Abulwafa, EM NOV 2011**

**Solitary, explosive and periodic solutions for electron acoustic solitary waves with non-thermal hot ions**

Author(s): [Elwakil, SA](#) (Elwakil, S. A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, E. M.)<sup>[1]</sup>; [El-Shewy, EK](#) (El-Shewy, E. K.)<sup>[1]</sup>; [Abd-El-Hamid, HM](#) (Abd-El-Hamid, H. M.)<sup>[1]</sup>

Source: ADVANCES IN SPACE RESEARCH Volume: 48 Issue: 10 Pages: 1578-1590 DOI: 10.1016/j.asr.2011.07.005 Published: NOV 15 2011

**Abstract:** A theoretical investigation has been made for electron acoustic waves propagating in a system of unmagnetized collisionless plasma consists of a cold electron fluid and ions with two different temperatures in which the hot ions obey the non-thermal distribution. The reductive perturbation method has been employed to derive the Korteweg-de Vries equation for small but finite amplitude electrostatic waves. It is found that the presence of the energetic population of non-thermal hot ions  $\delta$ , initial normalized equilibrium density of low temperature ions  $\mu$  and the ratio of temperatures of low temperature ions to high temperature ions  $\beta$  do not only significantly modify the basic properties of solitary structure, but also change the polarity of the solitary profiles. At the critical hot ions density, the KdV equation is not appropriate for describing the system. Hence, a new set of stretched coordinates is considered to derive the modified KdV equation. In the vicinity of the critical hot ions density, neither KdV nor modified KdV equation is appropriate for describing the electron acoustic waves. Therefore, a further modified KdV equation is derived. An algebraic method with computerized symbolic computation, which greatly exceeds the applicability of the existing tanh, extended tanh methods in obtaining a series of exact solutions of the various KdV-type equations, is used here. Numerical studies have been reveals different solutions e.g., bell-shaped solitary pulses, singular solitary "blowup" solutions, Jacobi elliptic doubly periodic wave, Weierstrass elliptic doubly periodic type solutions, in addition to explosive pulses. The results of the present investigation may be applicable to some plasma environments, such as Earth's magnetotail region. Crown copyright (C) 2011 Published by Elsevier Ltd. on behalf of COSPAR. All rights reserved.

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Author Keywords: Electron acoustic waves; Non-thermal hot ions; KdV-type equations; Explosive pulses

**KeyWords Plus:** PLASMA SHEET BOUNDARY; EARTHS MAGNETOTAIL; AURORAL-ZONE; NOISE; GENERATION; SOLITONS; REGION; SYSTEM

Reprint Address: El-Shewy, EK (reprint author), Mansoura Univ, Fac Sci, Theoret Phys Grp, Dept Phys, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Theoret Phys Grp, Dept Phys, Mansoura 35516, Egypt

**E-mail Address:** [e\\_k\\_el\\_shewy@mans.edu.eg](mailto:e_k_el_shewy@mans.edu.eg)

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**Abulwafa, EM MAR 2010**

**New Exact Travelling Wave Solutions of Nonlinear Coagulation Problem with Mass Loss**

Author(s): [El-Wakil, ESA](#) (El-Wakil, El-Said A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [Abdou, MA](#) (Abdou, Mohammed A.)<sup>[1,2]</sup>

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**Abstract:**

This paper suggests a generalized F-expansion method for constructing new exact travelling wave solutions of a nonlinear coagulation problem with mass loss. This method can be used as an alternative to obtain analytical and approximate solutions of different types of kernel which are applied in physics. The nonlinear kinetic equation, which is an integro differential equation, is transformed into a differential equation using Laplace's transformation. The inverse Laplace transformation of the solution gives the size distribution function of the system.

As a result, many exact travelling wave solutions are obtained which include new periodic wave solutions, trigonometric function solutions, and rational solutions. The method is straightforward and concise, and it can also be applied to other nonlinear evolution equations arising in mathematical physics.

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Author Keywords: Nonlinear Coagulation Problem; Mass Loss; New Exact Travelling Solutions; Laplace Transform

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Reprint Address: Abdou, MA (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Res Grp, Mansoura 35516, Egypt

[ 2 ] King Kahlid Univ, Dept Phys, Fac Educ Girls, Bisha, Saudi Arabia

**E-mail Address:** [m\\_abdou\\_eg@yahoo.com](mailto:m_abdou_eg@yahoo.com)

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Author(s): Abdou, M. A.  
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**Abulwafa, EM FEB 2009**

**An improved variational iteration method for solving coupled KdV and Boussinesq-like B(m, n) equations**

Author(s): [El-Wakil, SA](#) (El-Wakil, S. A.)<sup>[1]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>; [Abdou, MA](#) (Abdou, M. A.)<sup>[1,2]</sup>

Source: CHAOS SOLITONS & FRACTALS Volume: 39 Issue: 3 Pages: 1324-1334 DOI: 10.1016/j.chaos.2007.05.020 Published: FEB 15 2009

**Abstract:**

In this article, we implement a new, analytical technique: He's variational iteration Method for solving the coupled KdV and Boussinesq-like equations. In this method, first general Lagrange multipliers are introduced to construct correction functional for the problems. The multipliers in the functional can be identified optimally via the variational theory. Next the components of obtained iteration formulae defined by partial sum of other sequence, specially constructed according to Adomian's decomposition method (ADM). Also according to ADM We Used a partial sum of Adomian polynomials instead of nonlinear terms in iteration formulae. The initial approximations call be freely, chosen with possible Unknown constants, which can be determined by imposing the initial conditions. The results reveal that the proposed method is very effective and can be applied for other nonlinear problems. (C) 2007 Elsevier Ltd. All rights reserved.

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**KeyWords Plus:** ADOMIAN DECOMPOSITION METHOD; DIFFERENTIAL-EQUATIONS; NONLINEAR EQUATIONS; COMPACT SUPPORT; CONSTRUCTION

Reprint Address: Abdou, MA (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Res Grp, Mansoura 35516, Egypt

[ 2 ] King Khalid Univ, Fac Educ Girls, Dept Phys, Abha, Saudi Arabia

**E-mail Address:** [m\\_abdou\\_eg@yahoo.com](mailto:m_abdou_eg@yahoo.com)

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Author(s): Tari, Hafez; Ganji, D. D.; Rostamian, M.

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Author(s): Yusufoglu, Elcin

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**Abulwafa, EM OCT-NOV 2009**

**Application of the Exp-Function Method to the Riccati Equation and New Exact Solutions with Three Arbitrary Functions of Quantum Zakharov Equations**

Author(s): [Abdou, MA](#) (Abdou, Mohamed A.)<sup>[1,2]</sup>; [Abulwafa, EM](#) (Abulwafa, Essam M.)<sup>[1]</sup>

Source: ZEITSCHRIFT FUR NATURFORSCHUNG SECTION A-A JOURNAL OF PHYSICAL SCIENCES Volume: 63 Issue: 10-11 Pages: 646-652 Published: OCT-NOV 2008

**Abstract:**

The Exp-function method with the aid of the symbolic computational system is used for constructing generalized solitary solutions of the generalized Riccati equation. Based on the Riccati equation and its generalized solitary solutions, new exact solutions with three arbitrary functions of quantum Zakharov equations are obtained. It is shown that the Exp-function method provides a straightforward and important mathematical tool for nonlinear evolution equations in mathematical physics.

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Reprint Address: Abdou, MA (reprint author), Mansoura Univ, Fac Sci, Dept Phys, Theoret Res Grp, Mansoura 35516, Egypt.

**Addresses:**

[ 1 ] Mansoura Univ, Fac Sci, Dept Phys, Theoret Res Grp, Mansoura 35516, Egypt

[ 2 ] King Kahlid Univ, Dept Phys, Fac Educ Girls, Bisha, Saudi Arabia

E-mail Address: [m\\_abdou\\_eg@yahoo.com](mailto:m_abdou_eg@yahoo.com)

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